



General Certificate of Education (A-level)
June 2012

Mathematics

MS2B

(Specification 6360)

Statistics 2B

Mark Scheme

the www.mymathscloud.com

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MMM. My Maths Cloud Com

Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
√or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
–x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MS2B

			M	1S2B - AQA GCE Mark Scheme 2012 Jun
.				AS2B - AQA GCE Mark Scheme 2012 Jun. Thathsolo. Comments
Q	Solution	Marks	Total	Comments
1(a)	$x = \frac{2}{n} = \frac{15}{15} = \frac{36.4}{5}$	B1		oe
	$s^{2} = \frac{\sum (x - \overline{x})^{2}}{n - 1} = \frac{1407.6}{14} = 100.54$ (or $s = 10.03$)	В1		$\sigma^2 = 93.84$ or $\sigma = 9.687$ iff $\sigma/\sqrt{14}$ used below
	$t_{crit} = \pm 2.624$	В1		ignore signs for t_{crit} (allow $t = 2.62$) (if z used then $max(B1B1B0 M0A0A0)$
	98% CI for μ:			their $\overline{x} \pm t_{14} \times \frac{\text{their } s}{\sqrt{15}}$ or
	$36.4 \pm 2.624 \times \frac{s}{\sqrt{15}}$	M1		their $\overline{x} \pm t_{14} \times \frac{\text{their } \sigma}{\sqrt{14}}$
	(29.6, 43.2) 36.4 ± 6.8	A1ft		(allow any of the following for t_{14} : 1.345; 1.761; 2.145; 2.624; 2.977)
(b)	= 29.6,43.2	A1	6	cao
(10)	40.0 ∈ C.I. ⇒ no change	E1ft E1ft	2	Must refer to 40 (dep M1) Dep on previous mark
2()			8	
2(a)	$H_0: \mu = 4.0$ $H_1: \mu > 4.0$	B1		(both)
	$z_{calc} = \frac{4.2 - 4}{1.1 / \sqrt{40}}$	M1		Alternative: $P(\bar{X} > 4.2) = P(Z > 1.15)$ M1A1
	=1.15	A1		awrt
	$z_{crit} = 1.6449$	B1		= 1 - 0.87493 = 0.125 B1
				$0.125 > 0.05 \Rightarrow \text{ accept H}_0 \text{ Adep1}$
	Accept H ₀ [or Reject H ₁]	A1		Dep on B1M1B1
	Insufficient evidence at 5% level to support Julian's claim	E1	6	Dep on previous mark
(b)	Type II error. Accepted H_0 when H_0 was false (oe)	B1ft E1	2	Follow through on conclusion in (a) Dep on previous mark
				If Reject H ₀ in (a) then: No error (B1ft)
	Tota		8	Rejected H_0 when H_0 was false (oe) (E1)

MS2B

			N	MS2B - AQA GCE Mark Scheme 2012 Jun
3				MS2B - AQA GCE Mark Scheme 2012 Jun. Martis Clou
Q	Solution	Marks	Total	Comments
3(a)	for $-5 \le x \le 15$ $f(x) = \frac{d}{dx}F(x) = \frac{d}{dx}\left(\frac{x+5}{20}\right) = \frac{1}{20}$	B1	1	AG
	$P(X \ge 7) = 1 - F(7)$			Alternative:
	$=1-\frac{12}{20}$			Use of $f(x) = \frac{1}{20}$ or graph \Rightarrow
	$= \frac{2}{5} \text{ or } \left[\frac{8}{20}; \frac{4}{10}; 0.4 \right]$	B1	1	$P(X \ge 7) = \frac{1}{20} \times (15 - 7) = \frac{2}{5}$ (oe)
(ii)	$P(X \neq 7) = 1$	B1	1	cao
		B1	1	Alternative:
	2			$E(X) = \int_{-5}^{15} \frac{x}{20} dx = \left[\frac{x^2}{40} \right]_{-5}^{15}$
				$= \frac{1}{40} (225 - 25)$ $= \frac{1}{40} \times 200$ $= 5$ B1 (cao)
(iv)	$E(3X^{2}) = \int_{-5}^{15} \frac{3x^{2}}{20} dx$ (ignore limits)	M1		= 5 B1 (cao)
	$\left[\frac{x^3}{20}\right]_{-5}^{15}$			
	$\frac{1}{20}(3375+125)$ $168\frac{3}{4}+6\frac{1}{4}$	A1		correct limits seen / used
	=175 Alternative:	A1	3	(cao) (allow 174.9)
	Var $(X) = \frac{1}{12}(155)^2 = \frac{400}{12}$ (oe)	(B1)		$E(3X^2) = 3E(X^2)$
	$E(3X^2) = 3 \times \left[\frac{400}{12} + 5^2 \right]$	(M1)		$= 3 \times \left[\left\{ \text{their Var}(X) > 0 \right\} + \left\{ \text{their E}(X) \right\}^2 \right] used$
	L 12 J			(⇒ M1)
	=175	(A1)		

			N	IS2B - AQA GCE Mark Scheme 2012 Jun.
3				MS2B - AQA GCE Mark Scheme 2012 Jun. Martis Clou
Q	Solution	Marks	Total	Comments
4(a)	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	B2,1	2	B1 for any 1 correct (unsimplified) (B1) B2 all correct and simplified
(b)	P(fewer than 3 bedrooms are rented) $= P(R = 1,2) \Rightarrow$			Alternative: P(fewer than 3 not rented)
	P(fewer than 3 bedrooms not rented) $= 1 - P(R = 1,2)$	M1		= P(0, 1 or 2 not rented) = P(5, 4 or 3 are rented) = P(R = 3, 4, 5) M1 $p = 0.4 \times 0.6^2 + 0.4 \times 0.6^3 + 0.0296$
	=1-P(1 or 2 rooms are rented) =1- $(0.5 + 0.24)$ [their $0 < p(2) \le 0.4704$ value from table used]	m1		$p = 0.4 \times 0.6 + 0.4 \times 0.6 + 0.0296$ $= 0.144 + 0.0864 + 0.0296 m1$ [or their $p(3) + p(4) \le 0.4704$ value from table used]
	=1-0.74 = 0.26	A1	3	= 0.26 (cao) A1
() (*)			ı	[SC 0.74 for B1]
(c)(i)	$E(R) = 0.5 \times 1 + 0.4 \times 0.6 \times 2$ $+ 0.4 \times 0.6^{2} \times 3 + 0.4 \times 0.6^{3} \times 4$ $+ 0.0296 \times 5$ $= 0.5 \times 1 + 0.24 \times 2 + 0.144 \times 3 + 0.0864 \times 4$ $+ 0.0296 \times 5$	M1		$\sum_{i=1}^{5} r_{i} \times P(R = r_{i}) \text{ from their table}$
	$= 0.5 + 0.48 + 0.432 + 0.3456 + 0.148$ $\left[= \frac{1}{2} + \frac{12}{25} + \frac{54}{125} + \frac{216}{625} + \frac{37}{250} \right]$			(0.5+1.2576+0.148)
	$\therefore \mathrm{E}(R) = 1.9056$	A1	2	[awfw 1.9 to 1.91] $\left[1\frac{566}{625}\right]$
(ii)	$E(R^2) = 0.5 \times 1^2 + 0.4 \times 0.6 \times 2^2$		ı	$\left[0.5 + 0.96 + 1.296 + 1.3824 + 0.74\right]$
	$+0.4 \times 0.6^{2} \times 3^{2} + 0.4 \times 0.6^{3} \times 4^{2}$ $+0.0296 \times 5^{2}$ $E(R^{2}) = 4.8784$	В1		AG
	$Var(R) = 4.8784 - 1.9056^{2}$ (= 1.24708864)	M1	ľ	$4.8784 - \text{their E}^2(R)$
	=1.24708804 =1.25 (3sf)	A1	3	(awfw 1.23 to 1.25)

MS2B - AQA GCE Mark Scheme 2012 Jun. Marks Cloud Com MS2B Solution Marks Total Q (d) E(M) = 1250E(R) - 282 $=1250\times1.9056-282$ B1 cao =2100 $1250^2 \times \text{their Var}(R) > 0 \text{ in (c)(ii)}$ $Var(M) = 1250^2 \times [4.8784 - 1.9056^2]$ M1(1 948 473 to 1 953 125) $sd(M) = 1250 \times \sqrt{1.24708864}$ $sd(M) = \sqrt{1948437} = 1395.9$ $\left(\sqrt{1953125} = 1397.5\right)$ =1395.91(awfw 1395 to 1400) **A**1 3 13 Total

	MS2B - AQA GCE Mark Scheme 2012 Jun.					
				MS2B - AQA GCE Mark Scheme 2012 Jun. Comments 1-0.6530 = 0.347 (B1)		
В			 			
5(a)(i)	Solution P(Y < 0)	Marks	Total	Comments $1 - 0.6530 = 0.347 \text{ (B1)}$		
5(a)(1)	$P(X \ge 9) = 1 - P(X \le 8)$ = 1 - 0.5231			1-0.0530=0.547 (D1)		
	= 0.4769	B2,1	2	awfw 0.476 and 0.477		
(ii)	$P(5 < X < 10) = P(X \le 9) - P(X \le 5)$					
	=0.653-0.1496					
	= 0.5034	B3,2,1	3	awfw 0.503 to 0.504		
	ı			0.7634 - 0.1496 = 0.613 to 0.614 (B2) 0.6530 - 0.2562 = 0.397 to 0.398 (B2)		
	ı			0.0330 - 0.2302 - 0.397 to 0.398 (B2) 0.7634 - 0.2562 = 0.507 to 0.508 (B1)		
	ı			$\alpha - 0.1496 \text{ or } 0.653 - \alpha \text{ (B1) iff } 0$		
(b)	$P(Y < 2) = P(Y \le 1) = P(Y = 0 \text{ or } Y = 1)$			0.8 to 0.81 (B1)		
	$=e^{-1.5}+e^{-1.5}\times 1.5$	M1		(both)		
	[0.2231 + 0.3347]	1,11		(both)		
	= 0.5578254					
	= 0.558	A1	2	awfw 0.557 to 0.56		
(c)(i)	$\lambda = 8.5 + 1.5 = 10$	B1	1	Allow $P(10)$ or $Po(10)$		
(ii)	$P(T > 16) = 1 - P(T \le 16)$					
	=1-0.9730	M1				
	= 0.027	A1	2			
(iii)	$p = {}^{3}C_{2}0.027^{2} \times 0.973$	M1		for either term correct		
	$+0.027^{3}$ $=0.002128+0.00001968$	M1		for addition of the two correct terms		
	= 0.002128 + 0.00001988 = 0.0021 [4 dp]	A1	3	0.0021 or 0.0022 [iff M1M1 (+ 4dp)]		
	Alternative:	AI	,	0.0021 of 0.0022 [III MITMIT (+ 40p)]		
	$p = 1 - P(X \le 1)$					
	P(X=0) + P(X=1)					
	$= 0.973^3 + 3 \times 0.973^2 \times 0.027$	(M1)		for either term correct		
	= 0.921167 + 0.076685					
	p = 1 - 0.99785	(M1)		for 1 – [sum of two correct terms]		
	= 0.0021	(A1)		0.0021 or 0.0022 [iff M1M1 (+ 4dp)]		
	<u> </u>	<u> </u>	13			

MS2B

			N	MS2B - AQA GCE Mark Scheme 2012 Jun. Marks Cloud
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Q	Solution	Marks	Total	Comments
6(a)	H ₀ : No association between A level grade and class of degree H ₁ : Association between A level grade and class of degree	B1		At least H ₀ correct
	$\begin{array}{c cccc} O_i & E_i \\ \hline 20 & 11.6 \\ \hline 9 & 17.4 \\ \hline 36 & 36.4 \\ \hline 55 & 54.6 \\ \hline 22 & 28 \\ \hline 48 & 42 \\ \hline 2 & 4 \\ \hline 8 & 6 \\ \hline 200 & 200 \\ \end{array}$	M1		For E_i 's attempted
	Combine Class 2(ii) and 3	M1		For combining attempted
	20 11.6 8.4 6.0827 9 17.4 -8.4 4.0552 36 36.4 -0.4 0.0044 55 54.6 0.4 0.0029 24 32 -8 2.0 56 48 8 1.3333	M1		For final column attempted
	200 200 0 13.47	A1	1	(awrt 13.5)
	$v = 2 \chi_{1\%}^{2}(2) = 9.210$	B1 B1		$[\nu = 3 \text{ with } \chi^2 = 11.345 \text{ (B0B1ft)}]$
	Reject H ₀	A1		Dep on B1 M1M1M1 B1B1, not A1
	Fiona's belief justified	E1	9	Dep on B1 M1M1M1 B1B1, not A1
(b)	Fewer than expected gained a Class 1 degree having gained grade B in A-level Mathematics.	E1		
	More than expected gained a Class 2(ii) degree having gained grade B in A-level Mathematics.	E1	2	correct comments (see below)
	1 2(i) 2(ii) 3 comb 9 55 48 8 56 17.6 54.6 42 6 48 A B C D E			A: fewer than expected B: as expected C: more than expected D: more or similar than expected E: more than expected

				S2B - AQA GCE Mark Scheme 2012 Jun. That is cloud.
			M	1S2B - AQA GCE Mark Scheme 2012 Jun
IS2B	Solution	Marks	Total	Comments
Q 7(a)	Solution	WIATKS	Total	Comments
	1 160 08 08 07 07 08 08 08 04 03 04 03 04 03 04 04 05 06 06 07 07 08 08 08 08 08 08 08 08 08 08 08 08 08	B2,1	2	Straight line from $(1, 0.5)$ to $(3, \frac{1}{6})$. Horizontal straight line from $(3, \frac{1}{6})$ to $(5, \frac{1}{6})$.
(b)	$E(X) = \frac{1}{6} \int_{1}^{3} x(4-x) dx + \frac{1}{6} \int_{3}^{5} x dx$	M1		ignore limits (both parts attempted)
	$= \frac{1}{6} \left[2x^2 - \frac{x^3}{3} \right]_1^3 + \frac{1}{6} \left[\frac{x^2}{2} \right]_3^5$	A1		ignore limits (both correct)
	$= \frac{1}{6} \left[\left(18 - 9 \right) - \left(2 - \frac{1}{3} \right) \right] + \frac{1}{6} \left[\frac{25}{2} - \frac{9}{2} \right]$			
	$=\frac{1}{6}\left[7\frac{1}{3}+8\right]$	m1		use of correct limits. dep on M1A1
	$=2\frac{5}{9}$	A1	4	(AG)
(c)(i)	$P(X > 2.5) = \frac{1}{3} + \frac{1}{2} \times \left(0.25 + \frac{1}{6}\right) \times \frac{1}{2}$	M1		Or $1 - \int_{1}^{2.5} \frac{1}{6} (4 - x) dx = 1 - \left[\frac{1}{6} \left(4x - \frac{x^2}{2} \right) \right]^{2.5}$
	$=\frac{7}{16}$	A1	2	cao (0.4375)
(ii)	$P(1.5 < X < 4.5) = \frac{1}{2} \times \left(\frac{5}{12} + \frac{1}{6}\right) \times 1.5$ $+ (4.5 - 3) \times \frac{1}{6}$	M1		Or $\int_{1.5}^{3} \frac{1}{6} (4-x) dx + \int_{3}^{4.5} \frac{1}{6} dx$
	$=\frac{7}{16}+\frac{1}{4}$	A1		
	$=\frac{16}{16}$	A1	3	cao (= $\frac{11}{16}$ or 0.6875)
(iii)	P(X > 2.5 and 1.5 < X < 4.5) = $P(2.5 < X < 4.5)$			cao (= $\frac{11}{16}$ or 0.6875) $\int_{2.5}^{3} \frac{1}{6} (4-x) dx = \left[\frac{1}{6} \left(4x - \frac{x^2}{2} \right) \right]_{2.5}^{3} = \frac{5}{48}$
	$= \frac{1}{2} \times \left(0.25 + \frac{1}{6}\right) \times 0.5 + \frac{1}{4}$	M1		
	$= \frac{5}{48} + \frac{1}{4}$ $= \frac{17}{48}$	A1	2	cao (0.35416)
(iv)	$P(X > 2.5 1.5 < X < 4.5) = \frac{17/48}{11/16}$	M1		their $\frac{\text{(iii)}}{\text{(ii)}}$ iff $0 < p$'s < 1
	$=\frac{17}{33}$	A1	2	cao (allow 0.51)

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3				MS2B - AQA GCE Mark Scheme 2012 Jun. Comments	"SC/OU
Q	Solution	Marks	Total	Comments	
7(c)	Alternative Solution				
	(0				
	$\begin{bmatrix} 0 & x < 1 \end{bmatrix}$				
	$\int_{12}^{12} \left(x - 1 \right) (7 - x) 1 \le x < 3$				
	$F(x) = \begin{cases} 0 & x < 1 \\ \frac{1}{12}(x-1)(7-x) & 1 \le x < 3 \\ \frac{1}{6}(x+1) & 3 \le x < 5 \\ 1 & x \ge 5 \end{cases}$				
	$\begin{vmatrix} 6 \\ 1 \end{vmatrix}$				
	(1				
(i)	P(X > 2.5) = 1 - F(2.5)				
	$=1-\frac{1}{12}(2.5-1)(7-2.5)$	(M1)			
	1	(2.22)			
	$=1-\frac{1}{12}\times 1.5\times 4.5$				
	=1-0.5625				
	$=0.4375$ or $\frac{7}{16}$	(A1)		cao	
(!!)					
(11)	P(1.5 < X < 4.5) = F(4.5) - F(1.5)				
	$= \frac{1}{6} (4.5+1) - \frac{1}{12} (1.5-1) (7-1.5)$	(M1)			
	$=\frac{11}{12}-\frac{11}{48}$	(A1)			
	$\begin{vmatrix} 12 & 48 \\ = \frac{11}{16} & \text{or} & 0.6875 \end{vmatrix}$	()			
	$=\frac{16}{16}$ or 0.0873	(A1)		cao	
(iii)	P(X > 2.5 and 1.5 < X < 4.5)				
	= P(2.5 < X < 4.5)				
	= F(4.5) - F(2.5)				
		(M1)			
	$=\frac{11}{12} - \frac{9}{16}$	(1111)			
	$=\frac{17}{48}$	(A1)		cao	
(: **)	/				
	P(X > 2.5 1.5 < X < 4.5)				
	$= \frac{F(4.5) - F(2.5)}{F(4.5) - F(1.5)} \text{ or } \frac{\text{their (iii)}}{\text{their (ii)}}$	(M1)			
	. , , , , ,				
	$=\frac{\frac{17}{48}}{\frac{11}{16}}$				
	$=\frac{17}{33}$ or (allow $0.5\dot{1}$)	(A1)		cao	