# General Certificate of Education (A-level) June 2012 

Mathematics
MS2B

## (Specification 6360)

Statistics 2B

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## Key to mark scheme abbreviations

| M | mark is for method |
| :--- | :--- |
| m or dM | mark is dependent on one or more M marks and is for method |
| A | mark is dependent on M or m marks and is for accuracy |
| B | mark is independent of M or m marks and is for method and accuracy |
| E | mark is for explanation |
| Jor ft or F | follow through from previous incorrect result |
| CAO | correct answer only |
| CSO | correct solution only |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| A2,1 | 2 or 1 (or 0) accuracy marks |
| $-x$ EE | deduct $x$ marks for each error |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| c | candidate |
| sf | significant figure(s) |
| dp | decimal place(s) |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

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| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) |  | B1 <br> B1 <br> B1 <br> M1 <br> A1ft <br> A1 <br> E1ft <br> E1ft | 6 2 | oe <br> $\sigma^{2}=93.84$ or $\sigma=9.687$ <br> iff $\sigma / \sqrt{14}$ used below <br> ignore signs for $t_{\text {crit }}$ (allow $t=2.62$ ) <br> (if $z$ used then $\max (B 1 B 1 B 0$ M0A0A0) <br> their $\bar{x} \pm t_{14} \times \frac{\text { their } s}{\sqrt{15}}$ or <br> their $\bar{x} \pm t_{14} \times \frac{\text { their } \sigma}{\sqrt{14}}$ <br> (allow any of the following for $t_{14}$ : <br> 1.345; 1.761; 2.145; 2.624; 2.977) <br> cao <br> Must refer to 40 (dep M1) <br> Dep on previous mark |
|  |  |  | 8 |  |
| 2(a) | $\begin{aligned} \mathrm{H}_{0}: \mu & =4.0 \\ \mathrm{H}_{1}: \mu & >4.0 \\ z_{\text {calc }} & =\frac{4.2-4}{1.1 / \sqrt{40}} \\ & =1.15 \\ z_{\text {crit }} & =1.6449 \end{aligned}$ <br> Accept $\mathrm{H}_{0}$ [or Reject $\mathrm{H}_{1}$ ] <br> Insufficient evidence at 5\% level to support Julian's claim <br> Type II error. <br> Accepted $\mathrm{H}_{0}$ when $\mathrm{H}_{0}$ was false (oe) | B1 <br> M1 <br> A1 <br> B1 <br> A1 <br> E1 <br> B1ft <br> E1 | 6 2 | (both) <br> Alternative: $\mathrm{P}(\bar{X}>4.2)=\mathrm{P}(Z>1.15) \text { M1A1 }$ <br> awrt $=1-0.87493$ $=0.125 \quad \text { B1 }$ <br> $0.125>0.05 \Rightarrow$ accept $\mathrm{H}_{0}$ Adep1 <br> Dep on B1M1B1 <br> Dep on previous mark <br> Follow through on conclusion in (a) <br> Dep on previous mark <br> If Reject $\mathrm{H}_{0}$ in (a) then: <br> No error (B1ft) <br> Rejected $\mathrm{H}_{0}$ when $\mathrm{H}_{0}$ was false (oe) (E1) |
|  | Total |  | 8 |  |

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\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments <br>
\hline 3(a)
(b)(i) \& for $-5 \leq x \leq 15$
$$
\begin{aligned}
& \mathrm{f}(x)=\frac{\mathrm{d}}{\mathrm{~d} x} \mathrm{~F}(x)=\frac{\mathrm{d}}{\mathrm{~d} x}\left(\frac{x+5}{20}\right)=\frac{1}{20} \\
& \mathrm{P}(X \geq 7)=1-\mathrm{F}(7) \\
& = \\
& =1-\frac{12}{20} \\
& =\frac{2}{5} \text { or }\left[\frac{8}{20} ; \frac{4}{10} ; 0.4\right]
\end{aligned}
$$ \& B1

B1 \& 1

1 \& | AG |
| :--- |
| Alternative: |
| Use of $\mathrm{f}(x)=\frac{1}{20}$ or graph $\Rightarrow$ $\mathrm{P}(X \geq 7)=\frac{1}{20} \times(15-7)=\frac{2}{5}$ (oe) | <br>

\hline (ii) \& $\mathrm{P}(X \neq 7)=1$ \& B1 \& 1 \& cao <br>

\hline (iii) \& $$
\mathrm{E}(X)=\frac{1}{2}(-5+15)=5
$$ \& B1 \& 1 \& Alternative:

$$
\begin{aligned}
\mathrm{E}(X) & =\int_{-5}^{15} \frac{x}{20} \mathrm{~d} x=\left[\frac{x^{2}}{40}\right]_{-5}^{15} \\
& =\frac{1}{40}(225-25) \\
& =\frac{1}{40} \times 200 \\
& =5 \quad \text { B1 (cao) }
\end{aligned}
$$ <br>

\hline \multirow[t]{4}{*}{(iv)} \& \multirow[t]{4}{*}{| $\left.\begin{array}{c} \left.\mathrm{E}\left(3 X^{2}\right)=\int_{-5}^{15} \frac{3 x^{2}}{20} \mathrm{~d} x\right\} \text { (ignore limits) } \\ {\left[\frac{x^{3}}{20}\right]_{-5}^{15}} \\ \frac{1}{20}(3375+125) \\ 168 \frac{3}{4}+6 \frac{1}{4} \\ =175 \end{array}\right\}$ |
| :--- |
| Alternative: $\begin{aligned} & \operatorname{Var}(X)=\frac{1}{12}(15--5)^{2}=\frac{400}{12}(\mathrm{oe}) \\ & \mathrm{E}\left(3 X^{2}\right)=3 \times\left[\frac{400}{12}+5^{2}\right] \end{aligned}$ $=175$ |} \& M1

A1 \& \& correct limits seen / used <br>
\hline \& \& A1 \& 3 \& (cao) (allow 174.9) <br>

\hline \& \& | (B1) |
| :--- |
| (M1) | \& \& \[

$$
\begin{aligned}
& \mathrm{E}\left(3 X^{2}\right)=3 \mathrm{E}\left(X^{2}\right) \\
& =3 \times\left[\{\text { their } \operatorname{Var}(X)>0\}+\{\text { their } \mathrm{E}(X)\}^{2}\right] \text { used } \\
& (\Rightarrow \text { M1 })
\end{aligned}
$$
\] <br>

\hline \& \& (A1) \& \& <br>
\hline \& Total \& \& 7 \& <br>
\hline
\end{tabular}

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| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| (d) | $\begin{aligned} \mathrm{E}(M) & =1250 \mathrm{E}(R)-282 \\ & =1250 \times 1.9056-282 \\ & =2100 \end{aligned}$ | B1 |  | cao |
|  | $\begin{aligned} & \operatorname{Var}(M)=1250^{2} \times\left[4.8784-1.9056^{2}\right] \\ & \begin{aligned} \operatorname{sd}(M) & =1250 \times \sqrt{1.24708864} \\ & =1395.91 \end{aligned} \end{aligned}$ | M1 <br> A1 | 3 | $1250^{2} \times \text { their } \operatorname{Var}(R)>0 \text { in (c)(ii) }$ <br> (1948 473 to 1953 125) $\begin{aligned} \operatorname{sd}(M)=\sqrt{1948437} & =1395.9 \\ (\sqrt{1953125} & =1397.5) \end{aligned}$ <br> (awfw 1395 to 1400) |
|  | Total |  | 13 |  |

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| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 7(c) | Alternative Solution |  |  |  |
|  | $\mathrm{F}(x)= \begin{cases}0 & x<1 \\ \frac{1}{12}(x-1)(7-x) & 1 \leq x<3 \\ \frac{1}{6}(x+1) & 3 \leq x<5 \\ 1 & x \geq 5\end{cases}$ |  |  |  |
| (i) | $\begin{aligned} & \mathrm{P}(X>2.5)=1-\mathrm{F}(2.5) \\ & =1-\frac{1}{12}(2.5-1)(7-2.5) \\ & =1-\frac{1}{12} \times 1.5 \times 4.5 \\ & =1-0.5625 \\ & =0.4375 \text { or } \frac{7}{16} \end{aligned}$ | (M1) <br> (A1) |  | cao |
| (ii) | $\begin{aligned} & \mathrm{P}(1.5<X<4.5)=\mathrm{F}(4.5)-\mathrm{F}(1.5) \\ & =\frac{1}{6}(4.5+1)-\frac{1}{12}(1.5-1)(7-1.5) \\ & =\frac{11}{12}-\frac{11}{48} \\ & =\frac{11}{16} \text { or } 0.6875 \end{aligned}$ |  |  | cao |
| (iii) | $\begin{aligned} & \mathrm{P}(X>2.5 \text { and } 1.5<X<4.5) \\ & =\mathrm{P}(2.5<X<4.5) \\ & =\mathrm{F}(4.5)-\mathrm{F}(2.5) \\ & =\frac{11}{12}-\frac{9}{16} \\ & =\frac{17}{48} \end{aligned}$ | (M1) <br> (A1) |  | cao |
| (iv) | $\begin{aligned} & \mathrm{P}(X>2.5 \mid 1.5<X<4.5) \\ & =\frac{\mathrm{F}(4.5)-\mathrm{F}(2.5)}{\mathrm{F}(4.5)-\mathrm{F}(1.5)} \text { or } \frac{\text { their (iii) }}{\text { their (ii) }} \\ & =\frac{17 / 48}{11 / 16} \\ & \left.=\frac{17}{33} \text { or (allow } 0.5 \dot{1}\right) \end{aligned}$ | (M1) <br> (A1) |  | cao |
|  | Total |  | 15 |  |
|  | TOTAL |  | 75 |  |


[^0]:    Further copies of this Mark Scheme are available from: aqa.org.uk

